Relations between indirect tensile and flexural strengths for dry and plastic concretes

Relações entre resistências à tração indireta e à tração na flexão em concretos secos e plásticos

J. T. BALBO *
jotbalbo@usp.br

Abstract

Indirect tensile strength is not usually used for concrete mixtures proportioning and its technological control; flexural strength tests under third point loads arrangement are the pattern for such goals. Indeed, neither of such tests have the capability to set up the actual strength of a concrete slab since its response is under plane stress state. A critical review of the basic concepts on both kinds of tests allows foreseeing its limitations as well as how to overcome such shortcomings. At last correlations between the two kinds of tensile strength are presented considering dry and plastic concretes typically applied on paving, corroborating to former results achieved for plastic concretes.

Keywords: indirect tensile strength; flexural strength; brazilian split test.

Resumo

Medidas de resistência à tração indireta não são normalmente cotejadas na dosagem ou no controle tecnológico de concretos em pavimentação; os resultados de ensaios de resistência à tração na flexão, em especial com dois cutelos, são empregados para tais finalidades. Na realidade, nenhum de ambos os tipos de teste mede de fato a resistência real do concreto acabado na forma de placa por não representarem um componente estrutural que responde mecanicamente em estado plano de tensões. Uma revisão crítica dos conceitos relacionados a essas medidas de resistência permite claramente enxergar as limitações de cada uma das formas de aferição da resistência à tração e as maneiras de melhor encaminhar avaliações dessa natureza. Correlações entre ambas as medidas por meio de ensaios em concretos secos e plásticos específicos para pavimentação são apresentadas, corroborando com resultados anteriores obtidos para concretos plásticos.

Palavras-chave: resistência à tração na flexão; resistência à tração indireta; ensaio brasileiro.

* Universidade de São Paulo, Escola Politécnica, Departamento de Engenharia de Transportes, São Paulo, SP, Brasil

Received: 10 May 2013 • Accepted: 02 Oct 2013 • Available Online: 12 Dec 2013

© 2013 IBRACON
1. Introduction

In general, users of concretes made with hydraulic binders (for paving) have the concept that the material is not capable of resisting tensile stress since such strength is much lower than the compressive strength of concrete. However, from the point of view of cracking in early ages, the material would require investigation on tensile strength, since the drying shrinkage occurs exactly by imposing tensile stress fields on concrete in the early stages of hardening. Both aspects, curing and final property of hardened concrete are of special consideration in concrete paving when cracks resulting from tensile stresses must be strictly controlled: either shrinkage, by its purposeful induction in well-defined positions, or early manifestation of fatigue, when static strength intensely influences such behavior.

Trokellet al. [1] quotes studies that had previously established that, on average, the concrete tensile strength (direct) would be around 9% of its compressive strength. For concretes with low consumption of cement and dry Balbo [2] reached the same ratio (8.9%) studying cement treated crushed stone (named BGTC in paving, blend with well-graded particles size and cement consumption of 85 kg/m³, very close to compacted concrete, used in dams, and compacted in optimum moisture content in modified energy). However, the direct tensile tests have never been considered as an element for measuring concrete strength (Trokellet al. [1]) and they also encounter difficulties related to the heterogeneity of the specimens (Balbo [2]), which cause irregular rupture surfaces and sometimes outside the half-height of the sample, which according to Bazant and Cedolin[3], supported by Fracture Mechanics concepts, raise serious doubts on interpretation and acceptance of such results. Metha and Monteiro [4] claim that the fasteners (by gluing) of cylindrical specimens for the direct tensile testing impose stress fields at the ends that cannot be ignored on the results interpretation. In summary, the samples preparation for testing in direct tensile tests requires much more care and attention to details that may invalidate the results obtained (Newman and Bennett [5]).

Traditionally, with apparent legacy of the German European school (Balbo [6]), the measurement tensile tests in bending on prismatic specimens were quickly shaded, in the early 20 century in the metallurgical direction, according to Timoshenko ([11], cf. p. 106), was subject to compression opposing efforts through the same diameter of rocks (especially its vertical strata).

The theory for determining the stress field in cylinders or on disks is meant here in the third of the points on the thirds of the support span of the prismatic sample (two cleavers or third-point load, is meant here in the third of the span), the latter being more commonplace. In this article, the concrete tensile strength measured by Brazilian test (or split test) is usually greater than the direct tensile strength of the material (ASTM, 2004). Balbo [2] worked with both types of tests for the analysis of tensile strength of BGTC (cement treated crushed stone, as defined earlier), composed of well-graded aggregates and 4% of cement (CP II E 32) consumption by weight; for a supposed type of concrete with low cement consumption as the BGTC, in addition to confirm the assertion of ASTM mentioned above, a great difficulty of devising a test in direct tensile was observed, because, of course, during this type of test, samples broke in their weakest sections, namely in areas which have received less compaction energy (blows) during cylinders molding. For a series of identical samples, the value of $f_{tu}$ was 2.3 (with a coefficient of variation of 15%), while for direct tensile tests was obtained an average value of 1.2 (3.5% coefficient of variation), establishing the relationship that follows:

$$f_u = 0.52 	imes f_{tu}$$

(1)

Fusco [9] suggested for conventional concrete buildings the relation:

$$f_u = 0.85 	imes f_{tu}$$

(2)

Both equations above denote that the indirect tensile strength is higher than the direct tensile strength, which is usually explained by the fact that on the direct tensile test, the rupture plane is weaker and perpendicular to the direction of force application. In the Brazilian test (diametrical compression test or indirect tensile testing) the cylindrical sample, with extreme parallel plans, is subjected to a diametrical compression effort applied over a small width throughout its length, evenly, and this restricted load application area helps avoid the stresses concentration in addition to compensate small irregularities on the surface of the sample. Provetti and Michot[10] point out that this test allows a fracture test in mode I (pure stress) and that the stress field in the loading implementation plan is quite uniform, thus the test is fit for study of brittle materials fracture. Although it is not for everyday use in the concrete area, it is widely used on tensile strength measurement of asphalt concrete, aggregates and soils stabilized with hydraulic binders, and for analysis of rocks (especially its vertical strata).

The theory for determining the stress field in cylinders or on disks subject to compression opposing efforts through the same diametrical direction, according to Timoshenko ([11], cf. p. 106), was established by Heinrich Hertz in 1883. The tensile stress fields and observed theoretically that (from previous studies in Theory of Elasticity) the vertical distribution of stresses in the load implementation plan during the rupture of the samples would be uniform (Metha and Monteiro [4], cf. p. 74). The results were initially published in France and later adopted internationally, being commonly termed by “Brazilian test”. Currently, in Brazil this testing is regulated by NBR 7222 of the Brazilian Association of Technical Standards (ABNT [8]).

According to the American Society for Testing of Materials (ASTM), the tensile strength measured by Brazilian test (or split test) is usually greater than the direct tensile strength of the material (ASTM, 2004).

2. Determination of indirect tensile strength – Brazilian test

Fernando Luiz Lobo Barbosa Carneiro [7] faced with the need to check the ability of concrete rolls for the displacement of São Pedro Church in Rio de Janeiro (in 1943), employed the diametrical compression test on concrete rollers with 600 mm in diameter,
The Figure 2 shows isotension fringes patterns during a diametral disk compression test [12]. Unlike tensile test for concrete, the diametral compression test is considered to be useful and reliable for the estimation of the other conventional concrete strength, that is, bending tensile strength, and even to compression [1]. Thus,
there is no use reference of this test as a measure standard, but
as a means to estimate the other strengths given its execution
simplicity, in particular, if compared to the bending tensile test.
Krishnayya and Eisenstein [14] point out that, although the Brazil-
ian test cannot completely replace other types of tensile tests, it
allows more reliable determination of the tensile strength than the
direct tensile testing or double punch, while that for analysis of
real dams the bending test was inappropriate. Also, the bending
test would be most affected by compression planes of the material
in beams compared to the uniform distribution of tensile stress in
Brazilian test. Aydin and Basu [15], also with focus on uniform ten-
sile distribution, concluded that the test is quite useful for verifying
micro-structural damage conditions with flaws in rocks samples,
and weathering-related cracks. Fairhurst [16] indicated that, for
brittle materials, special attention would be required in the test ar-
rangement to avoid tangential stress at the edge of the cylinder,
because they would significantly change the stress distribution in
the sample, rendering the equations 3 and 4 above invalid.

3. Determination of bending tensile strength

The bending tensile test, depending on the use of one or two
cleavers, imposes different moments of rupture as described in

Figure 3. The basic rupture characteristics to each of the arrange-
ments shown are:

- One cleaver test: tendency to rupture in the central section
  of maximum bending moment, however not mandatory. The
  strength, if the rupture occurs outside this section, must be
  estimated linearly according to the bending moment that occurs
  in breaking distance considered from the nearest support;

- Double cleaver test: there’s one middle third of the beam request-
ed by constant bending moment, which gives greater assurance
  on stress measurement of lower magnitude, as the material
  breaks at a load to the vertical section theoretically weaker.

The Figure 4 shows a photoelasticity test result [14] for a bending
beam, similar to a double cleaver test, with support at the ends
of the beam of 25 mm high and 300 mm span between supports.
Fringes are parallel and their spacing and widths increase as it
approaches the span center, maximum tensile request zone on
lower fiber. The lack of parallelism of these fringes in this central
area of the bending beam relates not only to the curvature of the
beam (that leads to the tendency to rotate the fringes), but also
with the vertical deformations in the region that produce the shape
of elliptical arcs [14]. The tensile stress field during the bending
test is very different, and also for this point of view, the diametral
compression test.
Tensile stress at bending in the lower fiber of the beam is calculated under the good assumption that the neutral line is at mid-height of the cross-section and the stress distribution is triangular. The section of the beam has moment of inertia in relation to the position of neutral line \(bh^3/12\). The stress, at the lower fiber with distance \(z\) from the neutral line, is then calculated, for a single and double cleaver test, respectively, as follows:

\[
\sigma = \frac{M_{\text{max}}}{bb} \times \frac{z}{\frac{4}{bb^3} \times \frac{b}{2} = \frac{3P}{2bb^2}}
\]

In Brazil, the Standard for implementation of this testing is the NBR 12142 [17], in which specimens with cross-section of 150 x 150 mm are recommended. In the Standard ASTM C 78-09 [18], there is greater flexibility as to the size of the sample. In fact, Cervo [19] studying conventional high-performance concrete for paving, from dosages used for construction of two concrete floors, noted that there is no significant difference to make the use of 100 x 100 mm reduced dimensions specimens prohibitive, based on tests with the two dimensions of cross sections mentioned and in statistical study on the dispersion of the results (Figure 5). Tests of Kolmogorov-Smirnov on the results determined normal distributions with significance levels greater than 0.05. Strengths between two sets of specimens of the same concrete, but with different dimensions, underwent hypothesis testing “t” as in Student, confirming that there were no differences between the sets of data on bending tensile strength of these specimens. This generated great confidence, from then on, for the use of specimens of 100 x 100 mm dimensions in cross section, what has been incorporated since then in the technical community with regard to concrete paving in Brazil, using the same formulas for calculating as the NBR 12142 Standard [17]. The issues regarding the specimen dimension transcend a testing performance on specimens of dimensions apparently suitable, as it is discussed in the following item.

3.1 Dependence of tensile strength in the sample size

According to Troxell et al. [1], cf. p. 254) the scale effect on beams for bending tensile test takes place analogously to the case of specimens for compression tests: the larger the sample, the lower the rupture stress on the test. Bazant and Novak [20], systemizing numerical, analytical, and experimental researches about bending tensile test concluded that the common point between various surveys was that the bending tensile strength of the material would decrease with height increase (the cross-section) of the beams, although this scaling factor can be better verified in comparing the strengths between beams of clearly different heights (as 75 mm – minimum conventional height of the beam – and 250 mm, thickness of a simple concrete pavement). This is shown in Figure 6,

---

**Figure 5** – Relation between strengths for different beams (source: Cervo [19])

**Figure 6** – Tensile strengths behavior as function of sample highness or diameter
which indicates a decrease in bending tensile strength due to the increased in the cross section of the specimen (in this case, the height of the beam), in comparison with the constant tendency of tensile strength values through Brazilian test. These differences are intuitively understood when the stresses distribution field in Brazilian test are considered (see Figure 1), very uniform, as compared to the stress distributions on the pulled-out bottom flange of beams, as shown in Figure 7. The triangular distribution (approximate), below the neutral line, for two beams of different heights $h_1$ and $h_2$ cause angles of dip on the tensile stress distribution, respectively, of $\alpha$ and $\alpha'$, and $f_{ct,f}$ is confused with the applied stress ($\sigma_t$) in the figure. Stress variations along the triangular distributions presented are, respectively,

$$\Delta \sigma = \left( \frac{\partial \sigma_t}{\partial b} \right) = \frac{f_{ct,f}}{b_1}$$

(8)

$$\Delta \sigma' = \left( \frac{\partial \sigma_t}{\partial b} \right) = \frac{f_{ct,f}'}{b_2} = \frac{f_{ct,f}}{n \times b_1}$$

(9)

Notice that $h_2$ is greater than $h_1$ by $n$ times, where $n$ is a real number. Particularly, $\Delta \sigma'$ is smaller than $\Delta \sigma$; that is, the peer-to-peer tensile stress variation is smaller in height beam $h_2$ greater $n$ times than $h_1$. The physical consequence of this characteristic of stress distribution in beams of greater height is that the critical rupture stress has a much greater possibility of being imposed to a set of horizontal fiber planes in the face of beam bottom rather than just in its fiber or extreme face, which causes, because there’s a greater intensity of fracture in the fragile transition zone of the material, a more abrupt and rapid propagation of cracks toward the top of the beam, which has a material strength loss as an engineering measurement practical consequence. As a result of the non-uniformity of stresses distribution, it would increase the apparent material strength. Notice that, at the same pace as the diametral compression tensile test, uniform distributions of tensile strength generate smaller tensile rupture stresses, in such a way that the modeled behavior is intuitively understood by the graphic in Figure 7. Newman and Bennett [5] statistically determined that indirect tensile strength results are affected by the Length/Diameter ratio of the specimen. On their results, it was noted that the higher the Length/ Diameter ratio less the average strength of samples that ranged such relation from 0.5 to 1.0 (the average values obtained for sandstones for relations mentioned were of 9.5 and 8.2 MPa). Therefore, the opening set out by NBR 7222 [8] for conducting tests on specimens with the Length/Diameter ration between 1 and 2 must be taken with due caution since the cylindrical specimens molding traditionally preserves the ratio 2, which inductively makes us think in conservative result in tensile strength by diametral compression.

3.2 Actual state of stresses of slabs for pavement carpets and bases

In a plane stress state, a plate will have its horizontal stresses in directions $x$ and $y$, determined from the deformations imposed...
on the concrete, using the generalized Hooke’s law, as follows:

\[
\sigma_x = \frac{E}{(1-\mu^2)} \left( \varepsilon_x + \mu \varepsilon_y \right) \tag{10}
\]

\[
\sigma_y = \frac{E}{(1-\mu^2)} \left( \varepsilon_y + \mu \varepsilon_x \right) \tag{11}
\]

Imagining a plate of plane dimensions \(x\) and \(y\) long and an external load being applied vertically in the central region, by symmetry we can affirm that \(\varepsilon_y = \varepsilon_x = \varepsilon\) and therefore \(\sigma_x = \sigma_y\). Applying such equalities of deformations in the equation [11] the bending tensile stress is then determined in the direction \(x\), that is, to \(\mu = 0.15\):

\[
\sigma_x = \frac{E}{(1-\mu^2)} \left( \varepsilon_x + \mu \varepsilon_y \right) = \frac{E}{(1-\mu^2)} \left( \varepsilon + \mu \varepsilon \right) = \frac{E \varepsilon}{(1-\mu^2)} \left( \frac{1+\mu}{1-\mu} \right) = 1.1765 \frac{E \varepsilon}{(1-\mu)} \tag{12}
\]

Abstracting (as digression) the application of the same load in a bending volume where deformation in \(y\) direction tends to zero, it could be written from the equation [11]:

\[
\lim_{\varepsilon_y \to 0} \sigma_y = \frac{E}{(1-\mu^2)} \left( \varepsilon_y + \mu \varepsilon_x \right) = 1.023 \frac{E \varepsilon}{(1-\mu)} \tag{13}
\]

When compared the constants applied in the equations [12] and [13] it was concluded that the effect of the same load in a uniaxial stress state (when it is not plane as there is not contribution in the perpendicular direction, i.e., \(\varepsilon_y = 0\), or it is too small in relation to \(\varepsilon_x\) is to cause a rupture stress less than when there is a contribution of deformation in the opposite direction. Thus, transporting to a bending beam, a load causes theoretically, a less critical effect in terms of inducing stresses in the \(x\) direction that would occur if the same load was applied to a specimen causing stress distribution in a plane state (biaxial). Well, this means that, intuitively, the strength of a concrete slab, if measured by means of rupture stress in a plane stress state, is greater than the strength of the same concrete in unidirectional bending, as in the case of beams used for tests. In other words, it must be understood that the measures in the laboratory, at its current stage of practice and standards, are not able to create the adequate knowledge of what would be the real strength, or rather, the real load capacity of the concrete slab against vehicles action.

<table>
<thead>
<tr>
<th>Code</th>
<th>Particularities</th>
<th>Age</th>
<th># prismatic samples</th>
<th># cylindrical samples</th>
<th>Cement consumption (kg/m³)</th>
</tr>
</thead>
<tbody>
<tr>
<td>CCR I</td>
<td>100% of fine crushed sand</td>
<td>7 e 35</td>
<td>27</td>
<td>27</td>
<td>100</td>
</tr>
<tr>
<td>CCR II</td>
<td>100% fine river sand</td>
<td>7 e 35</td>
<td>9</td>
<td>9</td>
<td>100</td>
</tr>
<tr>
<td>CCR III</td>
<td>100% fine granulated blast slag sand</td>
<td>7 e 35</td>
<td>9</td>
<td>9</td>
<td>100</td>
</tr>
<tr>
<td>CCR IV</td>
<td>50% fine crushed sand + 50% fine granulated blast slag sand</td>
<td>7 e 35</td>
<td>6</td>
<td>6</td>
<td>100</td>
</tr>
<tr>
<td>CCR V</td>
<td>50% fine river sand + 50% fine granulated blast slag sand</td>
<td>7 e 35</td>
<td>6</td>
<td>6</td>
<td>100</td>
</tr>
<tr>
<td>CCR VI</td>
<td>50% fine milled asphalt mixture</td>
<td>35</td>
<td>3</td>
<td>3</td>
<td>100</td>
</tr>
<tr>
<td>CCR VII</td>
<td>50% medium size milled asphalt mixture</td>
<td>35</td>
<td>3</td>
<td>3</td>
<td>100</td>
</tr>
<tr>
<td>CCR VIII</td>
<td>50% coarse milled asphalt mixture</td>
<td>35</td>
<td>3</td>
<td>3</td>
<td>100</td>
</tr>
<tr>
<td>CCR IX</td>
<td>50% milled asphalt mixture (all sizes)</td>
<td>35</td>
<td>3</td>
<td>3</td>
<td>100</td>
</tr>
<tr>
<td>CCR X</td>
<td>20% ground rubber (\phi=4) mm</td>
<td>35</td>
<td>3</td>
<td>3</td>
<td>100</td>
</tr>
<tr>
<td>CCR XI</td>
<td>20% ground rubber (\phi=2) mm</td>
<td>35</td>
<td>3</td>
<td>3</td>
<td>100</td>
</tr>
<tr>
<td>CCR XII</td>
<td>20% ground rubber (\phi=0.4) mm</td>
<td>35</td>
<td>3</td>
<td>3</td>
<td>100</td>
</tr>
<tr>
<td>CCR XIII</td>
<td>10% ground rubber (\phi=4) mm</td>
<td>35</td>
<td>3</td>
<td>3</td>
<td>100</td>
</tr>
<tr>
<td>CCR XIV</td>
<td>10% ground rubber (\phi=2) mm</td>
<td>35</td>
<td>3</td>
<td>3</td>
<td>100</td>
</tr>
<tr>
<td>CCR XV</td>
<td>10% ground rubber (\phi=0.4) mm</td>
<td>35</td>
<td>3</td>
<td>3</td>
<td>100</td>
</tr>
<tr>
<td>CP I</td>
<td>Bridge deck concrete pavement</td>
<td>365</td>
<td>8</td>
<td>14</td>
<td>360</td>
</tr>
<tr>
<td>CP II</td>
<td>Concrete for Paving (1)</td>
<td>28</td>
<td>9</td>
<td>9</td>
<td>350</td>
</tr>
<tr>
<td>CP III</td>
<td>Concrete with 100% of coarse recycled concrete pavement aggregate</td>
<td>150</td>
<td>9</td>
<td>9</td>
<td>375</td>
</tr>
<tr>
<td>CP IV</td>
<td>Concrete for Paving (2)</td>
<td>150</td>
<td>3</td>
<td>3</td>
<td>360</td>
</tr>
<tr>
<td>CP V</td>
<td>Concrete for Paving (3)</td>
<td>150</td>
<td>3</td>
<td>3</td>
<td>420</td>
</tr>
<tr>
<td><strong>TOTALS</strong></td>
<td><strong>119</strong></td>
<td></td>
<td><strong>125</strong></td>
<td></td>
<td><strong>-</strong></td>
</tr>
</tbody>
</table>
Thus, the bending tensile tests are mere supporting players in the binomial structural sizing / mixing proportions of the concrete, being, in the case of mix proportioning, a potential capacity to measure the real strength of concrete slab overlooked, which operates in practice, in favor of safety, but at the expense of a relevant safety coefficient (or rather, a coefficient of “ignorance”) by the real ignorance of the problem. Furthermore, recent studies show that the bending tensile stress which produces the first fissure occurs at values of 35 to 40%, higher than those found in other tests, such as direct and indirect stress [21].

4. Studies of tensile strength on dry and plastic concretes

4.1 Concrete types studied

For the analyses presented herein, 244 specimens tested were considered, and part of which were from the same research lab, with the same equipment, partially previously published [22, 23, 24, 25]. The concretes examined were of conventional plastic types and high strength, as well as various types of dry concrete, including alternative aggregates; a portion of samples was obtained from a study of concrete produced with recycled aggregates in concrete pavement. All the results presented derive from the testing and previous research conducted and advised by the author (and previously unpublished), now being analyzed from the perspective of this article. Table 1 succinctly describes the concretes employed for carrying out tests in diametral compression and bending tensile.

4.2 Equipment and measures undertaken

The studied specimens had, in the case of cylindrical samples, 200 mm long by 100 mm in diameter, and the length / diameter ratio is therefore always kept. The prismatic specimens in all cases correspond to the dimensions 100 x 100 x 400 mm³. The tests were carried out at various ages of the concretes, as listed in Table 1. A static (hydraulic) squeezer was employed with capacity of 100 kN for tests on specimens, following the recommendations contained in the ASTM C496M-04 [26] and C293-08 [27] standards. The loads applied were acquired by means of electronic signals obtained with the instrumentation (use of load cells under the force application piston of the squeezer). The bending tensile tests were performed with the test arrangement of a single stiffener.

4.3 Relations between Strengths

Hammitt [28] proposed the following relation between the bending tensile strength and indirect tensile strength by diametral compression:

\[ f_{ct, f} = 1.02 \cdot f_{ct, sp} + 1.48 \ [MPa] \]  

(14)

Data presented in Figure 8 comprise the set of results obtained in several studies and used in this analysis, as mentioned above, and the regression equation between points (with R² = 0.88) is:

\[ f_{ct, f} = 1.16 \cdot f_{ct, sp} + 1.30 \ [MPa] \]  

(15)
Thus, it can be observed that the set of dry and plastic concretes considered herein, statistically treated in terms of its tensile strengths (bending and indirect), results in irrelevant change of the previously established relationship by Hammitt [28] for plastic concretes, and it is noteworthy to highlight that the results presented refer to bending tensile strength measured with a single cleaver testing. This study covers a broader range of strength for the generalization of the relationship sought between strengths. Note that all the points are above the line of equality between the parameters (45°) that means that the bending tensile stress on a cleaver have always resulted higher than the indirect tensile strength. In Table 2, there is a numerical comparison between 14 and 15 equations, which allows ensuring the use of both in case of dry concretes, at least in the range between 0.5 and 2.5 MPa of ultimate strength, when there is no important percentage variations between both. Table 3 shows direct relationships between values of indirect tensile strength and bending tensile strength to the same concretes, dry and plastic. It is observed that the dry concrete, naturally less mortared and more porous, has higher dispersion in results. The standard deviation obtained must be still considered high for molded samples in laboratory, which clearly indicates that the correlations should be cautiously considered when estimating bending tensile strength by diametral compression testing.

5. Conclusions

The issues about stress field distribution on concretes were addressed, because they have great interest in the field of plain concrete paving, as well as for the use of concrete foundations with asphaltic coatings. These stress fields, very different to the bending tensile test and indirect tensile test by diametral compression, ultimately result in values of tensile strength of the concrete different among themselves and hard to be correlated, given that the Brazilian test, more simple in practical and understandable terms on the stresses distribution, is not usual for technological control or mix proportioning of concretes for pavements. The tests presented in this article, which were carried out with dry compacted and plastic vibrated concrete, with materials that took very different inputs with each other, as slag or rubbers as sand particle fractions, recycled aggregates from construction and demolition waste, milled asphalt mixtures, high-performance and conventional concretes, in all cases, never revealed to the specimens, indirect tensile strength superior to the bending tensile strength. A relationship was also observed between both strengths four decades ago for plastic concretes, and a correlation was proposed for a broader range of studied concrete, validating the previous equation for dry concrete, of great interest for asphalt pavement bases and for concrete pavements (as the roller compacted concretes by and cement treated crushed stones).

The determination of strength by diametral compression, although it is non-standard as a mix proportioning and quality control parameter, can be gradually used for determination of concrete strength achieved at low ages (like a “thermometer” that can be expected from long-term strength), but especially for control of the finished concrete in track, given that the extraction of cylindrical specimens is very simple and has a destructive character much less relevant than the extraction of samples for making prismatic specimens in lab. It is suggested, in this case, to experimentally establish for each work a relationship between \( f_{ct,pl} \) and \( f_{ct,sp} \), avoiding the use of general correlations obtained from the previous technical literature, or even from earlier work records. Within the same work, there are possibilities, with systematic studies and constancy of materials, to reach the estimated models of good quality, as proposed by the study presented.

The continuous use of the technique of indirect tensile test by diametral compression can bring new lights in the future on how to take better advantage of a simple test preparation, whether from the point of view of molding or extraction, as well as considering the same laboratory apparatus for its performance. On the other hand, the uniform field of tensile stress distributions provides an important potential to the study, with less dispersion of results, of the modulus of elasticity of concrete in tensile, of great interest for various paving works with plain concrete or cemented materials for pavements bases.

The literature review points out that the strength measurements are affected by the scale effect, i.e. the size of the specimens. The studies make it clear that different formats of specimens and distinct tests impose stress fields for each case that implies tensile strength also unequal to the same concrete. The discussions presented clearly indicate that the concrete strength in the form of a working slab in a plane stresses state, which is the real world, can be quite different, being higher than the tensile strength measured by tests in a nearly uni-directional stresses state. Tensile strength in diametral compression tests is lower than those measured in bending beams, and the latter test is conservative with respect to the strength in plane stresses state, as seen in theory. What gives us the idea that there is still an open field to better specify concrete mix proportion and control criteria for pavements.
6. Acknowledgements

The author is grateful to the Brazilian Council for the Development of Science and Technology (CNPq) whom supported the research under the project 473498/2006-5.

7. References